Optimal deductibility:

Evidence from a bunching decomposition

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Overview

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 - New way of thinking about deduction policy choice.
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 - New method to decompose bunching in taxable income.
 - Exploit year-on-year change in bunching incentives.

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 - New way of thinking about deduction policy choice.
 - Under separability, deduction elasticity is key parameter.
- How can I identify the deduction elasticity?
 - New method to decompose bunching in taxable income.
 - Exploit year-on-year change in bunching incentives.
- What is the deduction elasticity in practice?
 - New admin. data to exploit Australian policy discontinuity.
 - Deduction elasticity –0.45 and gross-income elasticity 0.04.

Literature

Elasticity of taxable income (ETI)

Feldstein (1995, 1999); Slemrod (1998); Chetty (2009);
Doerrenberg, et al. (2015)

I show the ETI is not sufficient for a different tax instrument.

- Bunching
 - Saez (2010); Chetty, et al. (2011); Kleven and Waseem (2013)
 - I develop the first method to decompose bunching.
- Deductions
 - Doerrenberg, et al. (2015); Schächtele (2016); Paetzold (2017)
 - Best, et al. (2015); Bachas and Soto (2016)
 - I provide a new estimate of the deduction elasticity.

A model of optimal deductibility

Taxpayer's problem

Taxpayer chooses consumption, c, gross income, y, and deductions, d, given tax rate, τ , and deductibility rate, ρ , to maximise utility. Taxable income is $z = y - \rho d$.

$$\max_{c,y,d} \ u(c,y,d) \quad \text{ s.t. } c \leqslant y-d-\tau \cdot (y-\rho d),$$

which yields:

$$\frac{u_y}{u_d} = -\frac{1-\tau}{1-\rho\tau}.$$

Government's problem

The government chooses τ and ρ to maximise indirect utility, $\nu(\tau, \rho)$, and the external value of deductions, $\Phi(d)$.

$$\max_{\tau,\rho} \ \nu(\tau,\rho) + \Phi(d(\tau,\rho)) \quad \text{ s.t. } \tau \cdot (y-\rho d) \ge \mathsf{R}.$$

Identifying welfare impact of ρ requires variation in ρ :

$$\underbrace{\frac{\partial R}{\partial \rho} + \tau d}_{\text{Revenue leakage}} = \tau \cdot \left(\frac{\partial y}{\partial \rho} - \rho \cdot \frac{\partial d}{\partial \rho} \right),$$

but we don't commonly observe such variability.

Quasilinear, isoelastic & separable utility

- More common to observe variation in τ .
- But under quasilinear, isoelastic, and separable utility, variation in τ and in ρ have the same effect on deductions:

$$\begin{split} \mathfrak{u}(\mathfrak{y},\mathfrak{d}) &= \mathfrak{y} - \mathfrak{d} - \tau \cdot (\mathfrak{y} - \rho \mathfrak{d}) \\ &- \frac{\mathfrak{n}_{\mathfrak{y}}}{1 + 1/e_{\mathfrak{y}}} \cdot \left(\frac{\mathfrak{y}}{\mathfrak{n}_{\mathfrak{y}}}\right)^{1 + 1/e_{\mathfrak{y}}} + \frac{\mathfrak{n}_{\mathfrak{d}}}{1 + 1/e_{\mathfrak{d}}} \cdot \left(\frac{\mathfrak{d}}{\mathfrak{n}_{\mathfrak{d}}}\right)^{1 + 1/e_{\mathfrak{d}}} \end{split}$$

.

Optimal deductibility rate

With this functional form, the optimal deductibility rate is:

$$\rho^*(\tau) = \frac{1}{\tau} \cdot \frac{1 - \lambda^g - \Phi'(d) \cdot e_d}{1 - \lambda^g - \lambda^g \cdot e_d},$$

which has the Ramsey (1927) inverse-elasticity form.

A bunching decomposition method

Standard bunching method

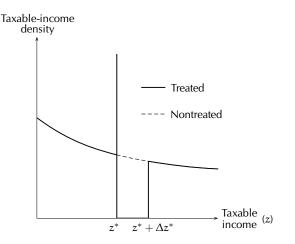


Figure: Densities with and without the notch

Bunching decomposition method

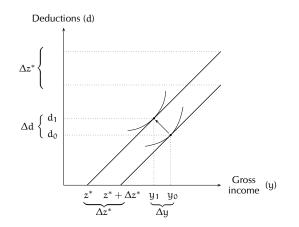


Figure: Changes in deductions and gross income due to the notch

Deriving the item elasticities

For an optimising buncher:

▶ in the absence of the notch:

$$y_0 = n_y (1-t)^{e_y}$$
 $d_0 = n_d (1-t)^{e_d}$

and in the presence of the notch:

$$\left(\frac{y_1}{n_y}\right)^{1/e_y} = \left(\frac{d_1}{n_d}\right)^{1/e_d},$$

such that $y_1 - d_1 = z^*$.

Deriving the item elasticities

These first-order conditions yield:

$$\frac{e_{\mathrm{y}}}{e_{\mathrm{d}}} = \frac{\ln \mathrm{y}_1 - \ln \mathrm{y}_0}{\ln \mathrm{d}_1 - \ln \mathrm{d}_0}.$$

Note the elasticity of taxable income is the weighted average:

$$\mathbf{e} = \frac{\mathbf{y}}{z} \cdot \mathbf{e}_{\mathbf{y}} - \frac{\mathbf{d}}{z} \cdot \mathbf{e}_{\mathbf{d}}$$

Combining these yields:

$$e_{\rm d} = e \cdot \frac{\ln\left(\frac{\Delta d}{d_0} + 1\right)}{\frac{y_0}{z_0} \cdot \ln\left(\frac{\Delta y}{y_0} + 1\right) - \frac{d_0}{z_0} \cdot \ln\left(\frac{\Delta d}{d_0} + 1\right)} \approx e \cdot \frac{\Delta d}{\Delta z} \cdot \frac{z}{\rm d}.$$

Deriving the item elasticities

Need to estimate:

$$\hat{\mathbf{e}}_{\mathrm{d}} = \hat{\mathbf{e}} \cdot \frac{\hat{\mathbb{E}}[\,\mathrm{d}_1 - \mathrm{d}_0]}{\hat{\mathbb{E}}[\,z_1 - z_0]} \cdot \frac{\hat{\mathbb{E}}[\,z_0]}{\hat{\mathbb{E}}[\,\mathrm{d}_0]},$$

all conditional on $z^* \leq z_0 \leq z^* + \Delta z^*$.

- ETI, ATEs, and average outcomes under nontreatment.
- Need to observe treatment and comparison groups.

Empirical analysis

Institutional settings

Medicare Levy Surcharge

- 1% tax on childless singles without private health insurance, and with taxable income above AU\$50,000.
- Different threshold for couples, based on joint income.
- In 2009, threshold was increased to \$70,000.

Institutional settings

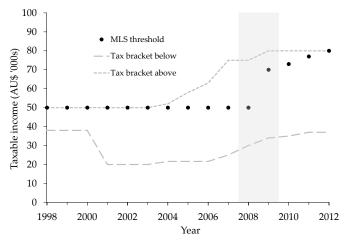


Figure: MLS threshold over time

- Use Australian Treasury administrative tax data.
- ▶ 16% sample (2 million observations in total).
- Exclude married people, those with children, and those covered by health insurance.
- Within \$2,250 income range considered and conditional on characteristics, dataset contains 80,000 observations.

Identification strategy

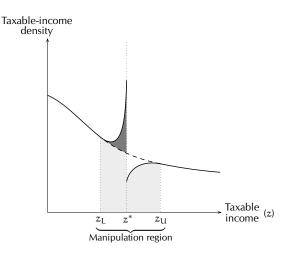


Figure: Bunching in the manipulation region.

Identification strategy

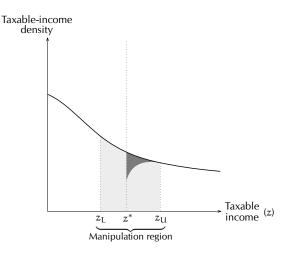
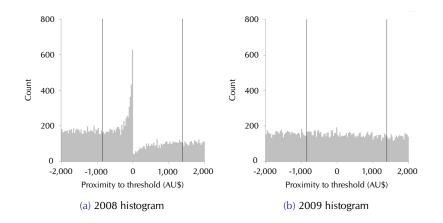


Figure: Bunching in the manipulation region.

Determining manipulation region



Determining manipulation region

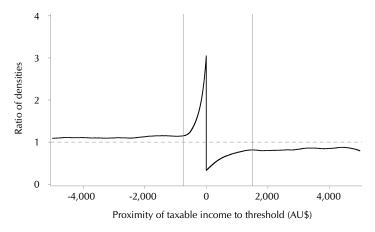


Figure: Density ratio from local-logit-regression predicted values

Determining placebo region

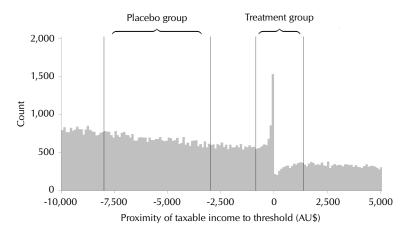


Figure: Density under treatment in treatment and placebo regions

Determining placebo region

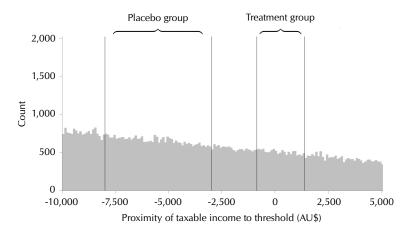
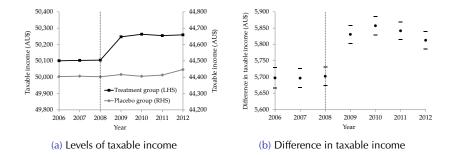
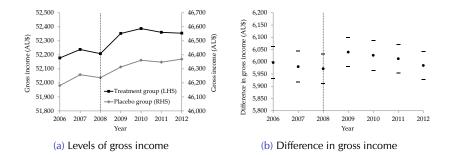


Figure: Density under nontreatment in treatment and placebo regions



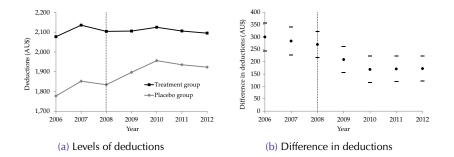
Pretrend-corrected DiD estmates:

- \$127.10 (26.61) among all taxpayers.
- \$526.73 (79.75) among bunchers only.



Pretrend-corrected DiD estmates:

- ▶ \$82.05 (56.74) among all taxpayers.
- \$340.03 (230.60) among bunchers only.



Pretrend-corrected DiD estmates:

► -\$45.05 (49.74) among all taxpayers.

-\$186.70 (215.55) among bunchers only.

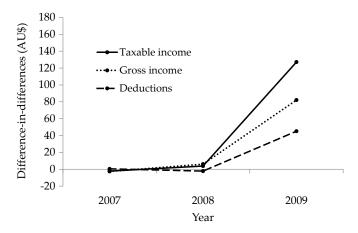


Figure: Pretrend-corrected differences-in-differences over time.

Bottom line

	% of TI	% of ΔTI	Item elasticity w.r.t.	
			Taxable	Net-of-tax
			income	rate
Gross income	104.71	64.55	0.62	0.04
Deductions	4.71	35.45	-7.53	-0.45

Table: Estimated item elasticities (ETI is 0.06).

- With 20% efficiency loss, marginal dollar of deductions requires 68¢ in external benefits for optimal full deductibility.
- If external benefits were 30¢, then $\rho^* = 0.34$.

Conclusion

- Under separability, tax-rate variation proxies for deductibility-rate variation.
- Decompose ETI via relative proportional changes of items and taxable income in bunching.
- Deductions account only for 5% of taxable income, but 35% of the response of taxable income to taxes.
- ▶ Deduction elasticity −0.45 and gross-income elasticity 0.04.
- Because deductions are granted at a high welfare cost, lowering deductibility is likely to raise welfare.

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